Nationellt prov, vårterminen 2022

Mathematics

Delprov C



Elevens namn och klass/grupp

Instructions – part C

Time for the test 60 minutes for part C.

Aids The allowed aids on part C are a formula sheet and a ruler.

Tasks For the tasks in this part, you are required to show your solutions.

Write your solutions in the test booklet.

If only the answer needs to be given in a task, this will be indicated by "Only answer required". For these tasks, no solutions need to be shown.

The maximum number of points you can be given for your answer is shown after each task.

Grading limits The test (parts B–D) gives a total maximum of 66 points.

Limit for test grade

E: At least 14 points.

D: At least 26 points, of which at least 9 points on level C or higher.

C: At least 34 points, of which at least 14 points on level C or higher.

B: At least 44 points, of which at least 4 points at level A.

A: At least 51 points, of which at least 8 points at level A.

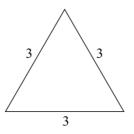


Illustrations: Jens Ahlbom

17. To construct a pattern similar to snowflakes, one can do what the Swedish mathematician Helge von Koch did.

Start from an equilateral triangle with 3 sides, see picture.





original triangle

Divide each side of the original triangle into three distances with equal lengths. The middle distance now forms the side of a new equilateral triangle. A new figure with a larger perimeter has now been formed, Figure 1. Repeat the procedure to create the next figure, Figure 2.

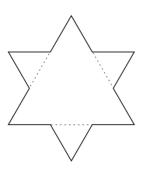


Figure 1

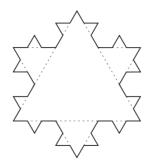
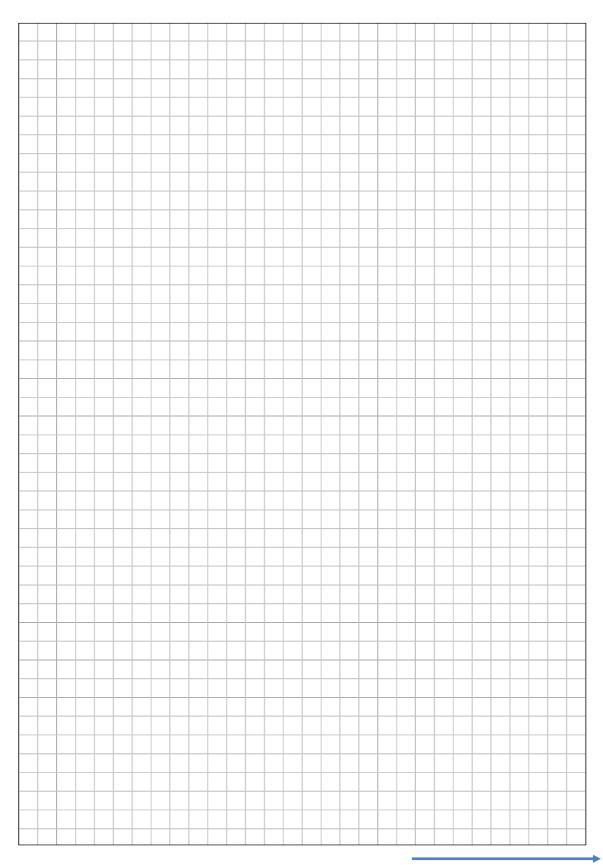


Figure 2

- a) The original triangle has a perimeter of 9. Calculate the perimeter of Figure 1.
- b) Calculate the perimeter of Figure 2.
- c) The perimeter increases with each figure. Calculate the change factor from Figure 1 to Figure 2.
- d) The perimeter increases exponentially with each figure. Write an exact formula for the perimeter *O* for Figure *n*.

DIGITAL DEVICES NOT ALLOWED

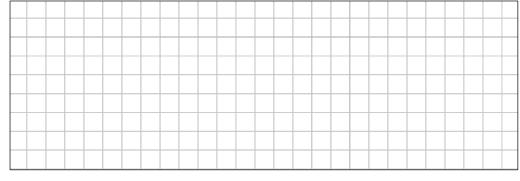


More tasks on the next page

DIGITAL DEVICES NOT ALLOWED

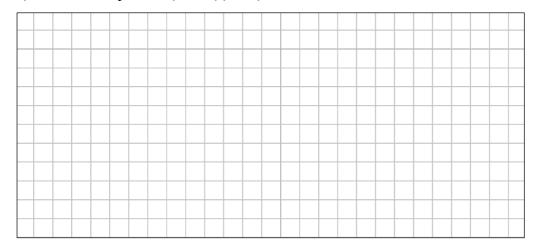
Solve the equation 15 - 4(x + 2) = 10x**18.**





b) Solve the equation $(2x - 5)(x + 3) = 2x^2 - 9$





Louise sees the following sign at the city swimming pool:

PRICES

Once-off single admission: SEK 59

Discount card for entry 10 times: SEK 399

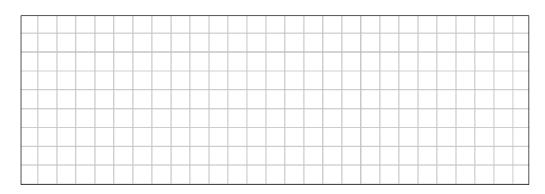
$$\frac{10 \times 59 - 399}{\text{with}}$$

Louise calculates $\frac{10 \times 59 - 399}{10}$ with her smartphone.

Louise gets the correct answer 19.1

Explain what Louise has calculated when she gets the answer 19.1

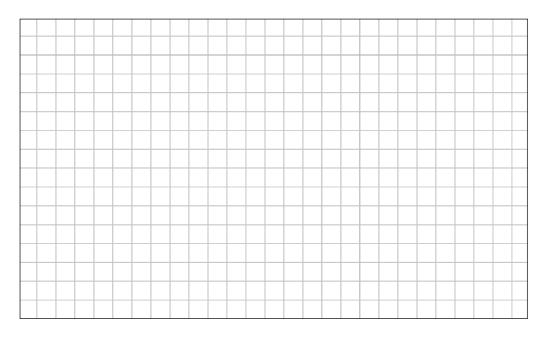
(0/1/0)



20. Ali attends the Natural Resource Use Programme and wants to mark off a 20 m^2 area to grow vegetables. The area should have the shape of a triangle with the base b metres and the height h metres. Ali wants to consider what the area might look like.

Determine a function for how base *b* depends on height *h* of Ali's area.

(0/1/0)



21. The width to height ratio of an A4 paper is $1:\sqrt{2}$ To obtain a paper in A5 format, one can split a sheet of A4 paper in half. Show that the width to height ratio of an A5 paper is also $1:\sqrt{2}$

(0/0/2)

