## Nationellt prov, vårterminen 2022

## Mathematics

Delprov D


## Instructions - part D

## Time for the test <br> 120 minutes for part D.

Aids The allowed aids on part D are digital devices, a formula sheet and a ruler.
Tasks For the tasks in this part, it is required of you to show your solutions. Write your solutions separately and turn them in together with the test booklet.

If only the answer needs to be shown in a task, this will be indicated by "Only answer required". For these tasks, no solutions need to be shown.

The maximum number of points you can be given for your answer is shown after each task.

Grading limits The test (parts B-D) gives a total maximum of 66 points.
Limit for test grade
E: At least 14 points.
D: At least 26 points, of which at least 9 points on level C or higher.
C: At least 34 points, of which at least 14 points on level C or higher.
B: At least 44 points, of which at least 4 points at level A.
A: At least 51 points, of which at least 8 points at level A.

Write your name and class/group on the papers you turn in.

22. Stina has deposited money in to a bank account with a fixed interest rate. The following function can be used to calculate how much money, in SEK, is in her bank account:
$f(x)=10000 \times 1.04^{x}$
where $x$ is the number of years after she has deposited the money into her bank account.
a) What interest rate did she receive from the bank?

Only answer required.
b) Calculate $f(5)$

Only answer required.
23. When the wind blows, it feels colder than actually shown on a thermometer. SMHI has published a table showing how the temperature is perceived depending upon actual temperature and wind speed.

|  |  | How the temperature is perceived |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Actual (at 0 m | ature ${ }^{\circ} \mathrm{C}$ | -15 | -10 | -5 | 0 | 5 | 10 |  |
|  | $2 \mathrm{~m} / \mathrm{s}$ | -20 | -14 | -8 | -2 | 3 | 9 |  |
| ¢ | $5 \mathrm{~m} / \mathrm{s}$ | -24 | -17 | -11 | -5 | 1 | 8 |  |
| \% | $10 \mathrm{~m} / \mathrm{s}$ | -27 | -20 | -14 | -7 | 0 | 6 | . |
| 듣 | $15 \mathrm{~m} / \mathrm{s}$ | -29 | -22 | -15 | -8 | -2 | 5 | $\stackrel{\square}{4}$ |
| 3 | $20 \mathrm{~m} / \mathrm{s}$ | -31 | -23 | -16 | -9 | -2 | 5 | - + |

a) How many degrees colder is a temperature of $-15^{\circ} \mathrm{C}$ perceived if the wind speed increases from $5 \mathrm{~m} / \mathrm{s}$ to $15 \mathrm{~m} / \mathrm{s}$ (according to the table)? Only answer required.
b) Is the relationship between wind speed and perceived temperature linear for the actual temperature $0^{\circ} \mathrm{C}$ ?
Justify.
24. Eskil has been offered a job at two different companies. He has been offered a basic salary every month throughout the year. And in addition, he would receive an extra supplement for each month that he is out on assignment.

| Employer | Basic salary <br> (SEK/month) | Extra supplement for <br> assignments (SEK/month) |
| :--- | :--- | :--- |
| Company A | 35000 | 10000 |
| Company B | 40000 | 3000 |

a) Calculate the annual salary with supplements for Eskil if he went to work for Company A and Company B respectively, if he is out on assignment for 5 months during one year.
b) Assume that Eskil would be out on assignment at Company A for as many months as he would be at Company B.
For the total annual salary to be higher at Company A, at a minimum how many full months will Eskil need to be out on assignment during one year?
25. Aida takes out a loan for SEK 20000 . The monthly interest rate is $3 \%$ and she wants to amortise SEK 1000 each month. For the purpose of calculating how much the monthly payment will be, Aida makes a spreadsheet.

|  | A | B | C | D | E |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Month | Remaining loan (SEK) | Interest rate/month (in decimals) | Amortisation/month (SEK) | Monthly payment (interest cost + amortisation in SEK) |
| 2 | January | 20000 | 0.03 | 1000 |  |
| 3 | February |  | 0.03 | 1000 |  |
| 4 | March |  |  |  |  |
| 5 | April |  |  |  |  |
| 6 | May |  |  |  |  |
| 7 | June |  |  |  |  |

a) What value is displayed in cell E2 when the monthly payment has been calculated? Only answer required.

Aida wants the spreadsheet to be usable irrespective of interest rate, loan amount and amortisation.
b) What formula should then be written in cell B3?

Only answer required.
c) What formula should then be written in cell E3 to calculate the monthly payment? Only answer required.
26. A triangle has the angles $A, B$ and $C$.

Angle $B$ is $72 \%$ smaller than angle $A$.
Angle $C$ is $60 \%$ larger than angle $A$.
Determine the size of each of the angles.
27. Samuel and Vera have had dinner together at a restaurant.

They pay a total of SEK 800 with the service charge of $12 \%$ included.
Before the service charge, how much did the dinner cost?
28. Hugo goes to an amusement park and plays on a number on the chocolate wheel.
The chocolate wheel has 20 fields, where one of the fields gives a win on each round of play.
a) What is the probability that he wins two consecutive rounds of play?
b) What is the probability that he wins at least one time if he plays seven rounds?

(0/2/1)
29. A newspaper article presents a formula for calculating the time difference in minutes if one drives the same distance at two different speeds.
$t=\left(\frac{1}{s_{1}}-\frac{1}{s_{2}}\right) \times d \times 60$
where
$t$ is the time difference in minutes
$s_{1}$ is the average speed $1 \mathrm{in} \mathrm{km} / \mathrm{h}$
$s_{2}$ is the average speed $2 \mathrm{in} \mathrm{km} / \mathrm{h}$
$d$ is the distance in kilometres

Kim drives a car to work. The distance to Kim's work is 20 km .
a) Use the formula to calculate the time difference in minutes if one day Kim drives at the average speed of $80 \mathrm{~km} / \mathrm{h}$ and on the second day instead drives at the average speed of $90 \mathrm{~km} / \mathrm{h}$ to work
b) Kim compares two other days' trips to work. Due to traffic, one of the average speeds was twice as high as the other.
The time difference between the two trips to work was 12 minutes. What average speeds did Kim drive those two days?
30. In a saline solution weighing $300 \mathrm{~g}, 12 \%$ of the weight is salt. How many grams of water will need to be added for the solution to instead contain $8 \%$ salt?
31. The number $x$ is somewhere between the numbers 17 and 23 . $x$ is $p \%$ greater than 17 and $p \%$ less than 23 .
Determine $x$.

