## Kursprov, vårterminen 2015

## Mathematics

Delprov D


## Instructions - Part D

Time for the test

Aids

## Tasks

## Grading limits

120 minutes for Part D.

Allowed aids on part D are digital devices, formula sheet and ruler.
This part consists of several tasks. The solutions are to be written on separate paper, which is to be submitted together with the test booklet. For most of the tasks in this part it is not enough to only give an answer, you also have to

- show your solutions
- explain/motivate your thinking
- draw figures when required.

For some tasks only the answer needs to be given. They are marked with "Only answer required".

The test (Part A-D) gives a total maximum of 93 points.
Limit for test grade
E: At least 20 points.
D: At least 35 points of which at least 13 points at level $C$ or higher.
C: At least 47 points of which at least 22 points at level $C$ or higher.
B: At least 59 points of which at least 7 points at level A.
A: At least 72 points of which at least 13 points at level A.

Name: $\qquad$
Date of birth: $\qquad$
Program: $\qquad$ Class: $\qquad$

Also write your name, date of birth, program and class on the sheets you hand in.
17. Amina has taken out an interest-only mortgage of SEK 800000.

How much does she pay in interest per month if the annual interest rate is $3.6 \%$ ?
18. Suppose that the time is 9 o'clock in the morning. What will the time be 1000 hours later?
19. Kalle's class is collecting money to the class fund and wants to organise a school disco. They have found a place that costs SEK 500 to rent and a DJ with a sound system that costs SEK 1 500. They are going to sell tickets for SEK 50 per ticket.

a) How big a profit will the class make if they manage to sell 100 tickets?
b) State a function $V(x)$ that shows the class' profit/loss after $x$ number of sold tickets.
c) There will be a maximum of 200 paying guests at the disco. Determine the range of the function.
20. The corners of a triangle have the coordinates $(1,2),(3,4)$ and $(2,5)$. Reflect the triangle in the line $y=x+1$ and state the coordinates of the reflected triangle's corners.
21. You roll two dice. One die has four sides, numbered 1 to 4 . The other die has six sides, numbered 1 to 6 . Show that the probability of at least one of the dice showing a "three" is $3 / 8$.

22. In 2014, the price of electricity was 27 öre per kWh.

That was $40 \%$ lower than the year before.
How much did 1 kWh cost in 2013?

$$
1 \mathrm{kWh}=1 \text { kilowatt hour }
$$

23. In the equality $\frac{15}{c}=\frac{d}{4} c$ and $d$ are positive integers.
a) Give one suggestion for what values $c$ and $d$ might have so that the equality holds. Only answer required.
b) Investigate what values $c$ and $d$ can have so that equality will hold.
24. Kim and Alex are comparing results from the school election.

Kim says that an increase from $16 \%$ to $19 \%$ is greater than an increase from $32 \%$ to $36 \%$. Alex says that it is the other way around. Can they both be right? Motivate.
25. Emre is going to take out a new mobile phone subscription. His grandmother lives in Turkey and in an average month Emre makes 3 hours of domestic calls and 2 hours of international calls.
a) Which of the following subscriptions is the cheapest for him?

|  | Subscription A | Subscription B |
| :--- | :--- | :--- |
| Fixed monthly rate | SEK 100 | SEK 289 |
| Call rate, domestic | SEK $0.49 /$ min | SEK $0.49 /$ min |
| Call rate, international | SEK $4.69 / \mathrm{min}$ | SEK $0.49 / \mathrm{min}$ |

b) Write one formula for Subscription A and one for Subscription B, in which $T$ is the total cost per month, $d$ is the number of minutes of domestic calls, and $i$ is the number of minutes of international calls.
c) For which call durations (domestic and international) do the two subscriptions cost the same?
26. Frida takes out an SMS loan of SEK 1000 . The loan is to be repaid after one month and the monthly interest rate is $20 \%$. At the end of the month Frida cannot afford to pay her debt.

In order to pay her debt she takes out a new SMS loan for the whole amount she owes. The new loan has the same monthly interest rate.

Frida continues to borrow in the same way every month. How large is Frida's debt one year after she took out her first SMS loan?
27. The graph shows the price development for one kilogramme of coffee in Sweden. According to an index series, the index for the coffee price was 330 in the year 2011. What year was the index series' base year?

28. Show that the area of the large circle is twice as large as the area of the small circle. M is the centre point of the large circle, and $m$ is the centre point of the small circle.


